

-  $x \downarrow$

$$\begin{aligned} X_i &= 4000\text{m} & V_f &= ? \\ V_i &= -20\text{m/s} & t_f &= ? \\ t_i &= 0\text{s} \\ a &= 9.80\text{m/s}^2 \end{aligned}$$

——  $X_f = 0\text{m}$   
 What will the velocity be  
 at 1500m from the ground

$$\begin{aligned} X_i &= 4000\text{m} & t_i &= 0\text{s} & V_i &= -20\text{m/s} \\ X_f &= 1500\text{m} & t_f &= ? & V_f &= ? & a &= 9.8\text{m/s}^2 \end{aligned}$$

$$V_f^2 = V_i^2 + 2a\Delta X$$

$$\begin{aligned} V_f &= \left[ V_i^2 + 2a\Delta X \right]^{1/2} \\ &= \left[ (-20\text{m/s})^2 + 2(-9.8\text{m/s}^2)(1500\text{m} - 4000\text{m}) \right]^{1/2} \end{aligned}$$

$$\boxed{V_f = -222\text{m/s}}$$

$t_f = ?$   $V_f = V_i + a\Delta t$

$$\Delta t = \frac{V_f - V_i}{a} = \frac{-222.26\text{m/s} - (-20\text{m/s})}{-9.8\text{m/s}^2}$$

$t_i = 0 \Rightarrow \boxed{t_f = 20.6\text{s}}$

Finding  $t_f$  using Eq'n. 3

$$X_f = X_i + V_i\Delta t + \frac{1}{2}a\Delta t^2$$

$$\frac{1}{2}a\Delta t^2 + V_i\Delta t + (X_i - X_f) = 0$$

Quadratic Eq'n.  $\frac{1}{2}(-9.8\text{m/s}^2)\Delta t^2 - (20\text{m/s})\Delta t + 2500\text{m} = 0$

Quadratic Formula  $\Delta t = \frac{-b \pm [b^2 - 4ac]^{1/2}}{2a}$

$$\Delta t = \frac{20\text{m/s} \pm [(-20\text{m/s})^2 - 4(-4.9\text{m/s}^2)(2500\text{m})]^{1/2}}{2(-4.9\text{m/s}^2)}$$

$$\Delta t = -2.04\text{s} \pm 22.68\text{s}$$

Pick the positive root:  $t_i = 0$   $\boxed{t_f = 20.6\text{s}}$